# Hedging Strategies for Load-Serving Entities in Wholesale Electricity Markets

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Figure: Supply and Demand in Electricity Markets



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#### Restructuring of Electricity Markets

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- $\bullet$  2000: Wholesale prices of  $\approx$  150 USD/MWh in California
- **Introduction of Demand Response and contracts between utilities and generators**

- Electric utilities face price and quantity risks:
	- Provide electricity to end users
	- Locational Marginal Prices (LMPs)
	- Energy storage prohibitively costly
- **Generating companies face similar**



- Contracts between generators and utility to alleviate risk?
- **Hedging Instruments** 
	- One-to-one contracts/options between generators and the utility
	- Demand Response to relay risk from utility to end-users
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#### Utility  $\leftrightarrow$  Users

• Demand Response: Give incentive  $r \in \mathbb{R}_+$  to user. User reduces consumption by  $h(r) \in \mathbb{R}_+$ 

$$
\Pi_{\text{DR}} = (\lambda_f - \lambda_s)d(r) - r
$$





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- Wholesale price  $\lambda_s$ , CDF G
- Fixed residential tariff  $\lambda_f$
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### Influence of Uncertainty

#### Influence of Distribution Tail

• Conditional Value-at-Risk (CVaR) given confidence level  $\alpha \in (0,1)$  and CDF  $F(\cdot)$  of random variable X:

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\mathsf{CVaR}_{\alpha}(X) = \mathbb{E}[X \mid X \geq F^{-1}(\alpha)]
$$

 $\bullet$  Expected loss in the worst  $(1-\alpha)\cdot 100\%$  of cases / expectation of  $(1-\alpha)$ 

$$
\mathbb{E}[\Pi_F^*] = \lambda_f \mathbb{E}[d] - \bar{\lambda}_F \cdot \text{CVaR}_{\alpha_F}(d)
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#### Influence of Statistical Dispersion

- Intuition: The more spread out  $F(\cdot)$ , the lower the expected profit.
- $\bullet$  For simplicity: Express optimal profits in terms of standard deviation  $\sigma$  of uniform

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\mathbb{E}[\Pi_{\Gamma}^{*}] = \lambda_{\Gamma} \mathbb{E}[d] - \bar{\lambda}_{\Gamma} d_{\min} - \sqrt{3} \mathbb{E}[\lambda_{s}](1 - \alpha_{\Gamma}^{2}) \sigma
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# Data Generation for Simulations

#### Demand Distribution

Aggregate hourly smart meter data, provided by OhmConnect, Inc.



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#### Distribution of LMPs

• Scrape 5-minute LMPs from public sources; aggregate to 60-minute values



# Pairwise Comparison (I)

#### DR vs. Forward Contract



# Pairwise Comparison (II)

DR vs. Call



# Pairwise Comparison (III)

#### Forward Contract vs. Call



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# THANK YOU! QUESTIONS?