

# Residential Demand Response Targeting Using Machine Learning with Observational Data

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# Residential Demand Response

## Background

- Reliable grid operation is dependent on adequate supply and flexible resources
- 2009: CAISO proposes “**Proxy Demand Resource Product**” to “facilitate the participation of existing retail demand programs in the ISO market”
- Proxy Demand Resources (PDRs) offer bids to reflect flexibility to adjust load in response to market schedules
- July 2015: CPUC Resolution E-4728 approves an auction mechanism for demand response capacity, called the “**Demand Response Auction Mechanism (DRAM)**”
- (Residential) Demand Response Providers with the ability to aggregate customers capable of reducing load participate in the ISO day-ahead, real-time ancillary services market
- Utilities can obtain resource adequacy through residential resources
- Benchmarking of reduction potential by using consumption “baselines”

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# Estimating the Counterfactual

- Causal Inference: Set of users  $\mathcal{I} = \{1, \dots, N\}$ , each user has observed outcomes  $\mathbf{y}_i = \{y_{i1}, \dots, y_{i\tau}\}$ , corresponding covariates  $X_i = \{\mathbf{x}_{i1}, \dots, \mathbf{x}_{i\tau}\}$ , and binary treatment indicator  $D_{it}$
- Potential outcomes framework (Rubin, 1974) and fundamental problem of causal inference:

$$y_{it} = y_{it}^0 + D_{it}(y_{it}^1 - y_{it}^0) \quad \forall i \in \mathcal{I}, t \in \{1, \dots, \tau\}$$

- That is, either the treatment outcome  $y_{it}^1$  or the control outcome  $y_{it}^0$  can be observed, but never both.
- Individual treatment effect  $\beta_i$  (ITE) and average treatment effect (ATE)  $\mu$ :

$$\beta_i = \mathbb{E}[y_{it}^1 - y_{it}^0] = \frac{1}{|\mathcal{T}_i|} \sum_{j \in \mathcal{T}_i} (y_{ij}^1 - y_{ij}^0) \quad \mu = \frac{1}{N} \sum_{i \in \mathcal{I}} \beta_i$$

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- $\Rightarrow$  Estimate counterfactuals!

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# Measuring Reduction in Consumption

- Estimate the demand reduction by using suitable baselines (counterfactuals)

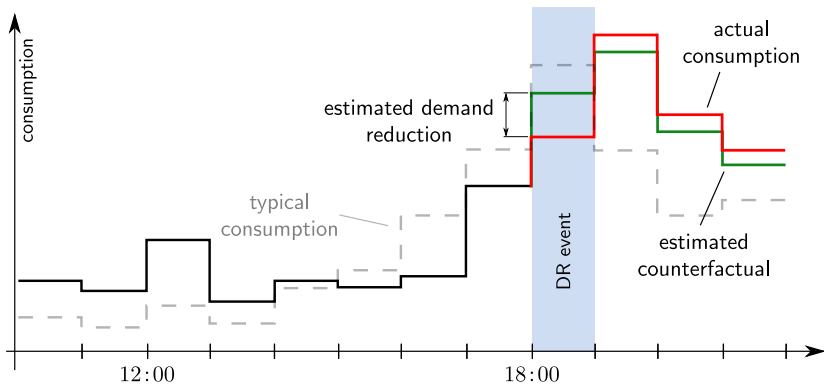


Figure: Estimated counterfactual vs. actual consumption<sup>1</sup>

<sup>1</sup>Courtesy of Maximilian Balandat

# Today's Talk

## Agenda

- Motivation for Residential Demand Response (done)
- Related work
- Methods for estimating the counterfactual consumption
  - (Black box) Machine Learning methods
- Estimation of average treatment effects
- User-specific analysis
  - Typical load shapes
  - Variation of ITE across users
- Case study on DR program in California
- Conclusion and further work

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## Economics

- Experimental Settings (Randomized Control Trials): Measure the counterfactual
- Non-experimental settings: Obtain non-experimental estimates of the counterfactual<sup>23</sup>

## Engineering

- Short-term load forecasting (STLF):
  - Effect of aggregation size
  - Estimation accuracy
- Load shape analysis
- Load scheduling
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# Machine Learning for Short-Term Load Forecasting

- Basic outcome model:

$$y_{it} = f_i(\mathbf{x}_{it}) + D_{it}\beta_i + \epsilon_{it}$$

- Treatment and control data:

$$\mathcal{D}_{i,t} = \{(\mathbf{x}_{it}, y_{it}) \mid t \in \mathcal{T}_i\}$$

$$\mathcal{T}_i = \{t \in \mathbb{T} \mid D_{it} = 1\}$$

$$\mathcal{D}_{i,c} = \{(\mathbf{x}_{it}, y_{it}) \mid t \in \mathcal{C}_i\}$$

$$\mathcal{C}_i = \{t \in \mathbb{T} \mid D_{it} = 0\}$$

- Two-step strategy to estimate counterfactuals:

- Estimate conditional mean function  $\hat{f}_i(\cdot) : \mathbb{R}^n \mapsto \mathbb{R}$  on control data  $\mathcal{D}_{i,c}$  with *any* regression method
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- Regression methods used:

- CAISO 10-in-10 Baseline (BL)
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## Further Analyses

### Statistical Hypothesis Testing

- Wilcoxon Signed Rank Test (paired difference test) to compare  $\{y_{ij}^1 \mid j \in \mathcal{T}_i\}$  and  $\{\hat{y}_{ij}^0 \mid j \in \mathcal{T}_i\}$
- Null hypothesis  $H_0$ : The samples  $\{y_{ij}^1 \mid j \in \mathcal{T}_i\}$  and  $\{\hat{y}_{ij}^0 \mid j \in \mathcal{T}_i\}$  are drawn from the *same* distribution

$$U \sim \mathcal{N}(\mu, \sigma^2) \quad \mu = 0, \sigma^2 = \frac{|\mathcal{T}_i|(|\mathcal{T}_i| + 1)(2|\mathcal{T}_i| + 1)}{6} \quad \text{if } |\mathcal{T}_i| \text{ large enough}$$

- For each user  $i \in \mathcal{I}$ , determine rank and test statistic to determine a  $p$ -value

### Variability of Load Shapes

- Use  $k$ -means clustering on daily load shapes to find characteristic profiles  $\{C_1, \dots, C_k\}$
- Use *entropy* measure  $H_i$  to characterize variability of consumption behavior:

$$H_i = - \sum_{s=1}^k p_s(C_s) \log(p_s(C_s))$$

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# Case Study on DR Program

- Hourly smart meter time series data on residential customers in California
- Hourly ambient air temperature scraped from public data sources
- Data preprocessing
  - Drop obvious outliers
  - Drop negative consumption data (and all users on net energy metering)
- Split cleaned hourly consumption data into three sets:
  - $\mathcal{D}_{i,t}$ , i.e. the treatment data set
  - $\mathcal{D}_{i,p} \subset \mathcal{D}_{i,c}$ , the placebo treatment set
  - $\mathcal{D}_{i,tr} = \mathcal{D}_{i,c} \setminus \mathcal{D}_{i,p}$ , the training data set
- Choose covariates:
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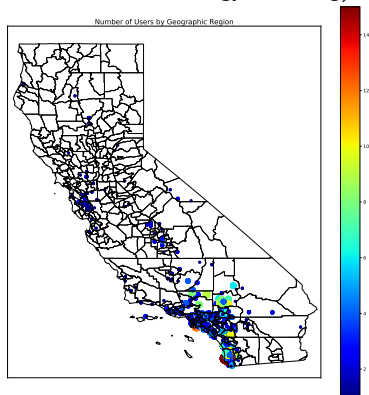


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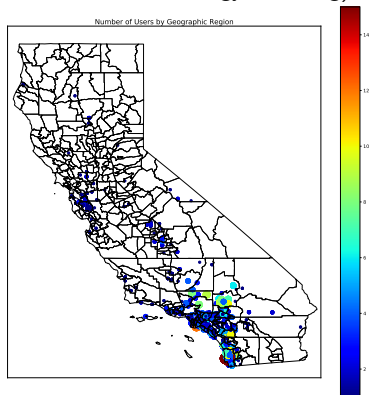


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  - $\mathcal{D}_{i,p} \subset \mathcal{D}_{i,c}$ , the placebo treatment set
  - $\mathcal{D}_{i,tr} = \mathcal{D}_{i,c} \setminus \mathcal{D}_{i,p}$ , the training data set
- Choose covariates:
  - Hour of the day as a categorical variable
  - Ambient air temperature
  - Previous  $n_{ar}$  hourly consumption values

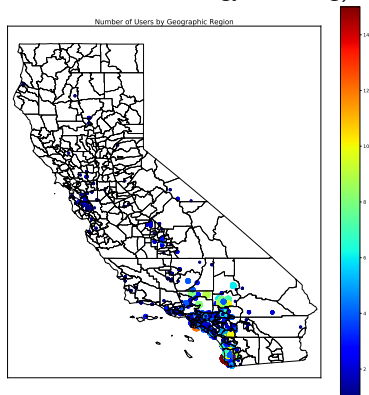


Figure: Distribution of Users



## Case Study on DR Program (cont'd)

### Prediction Accuracy

- Define Mean Absolute Percentage Error (MAPE) as metric for prediction accuracy:

$$\text{MAPE} = \frac{1}{|\mathcal{D}_{i,v}|} \sum_{j \in \mathcal{D}_{i,v}} \left| \frac{\hat{f}_i(\mathbf{x}_{ij}) - y_{ij}}{y_{ij}} \right| \cdot 100\%$$

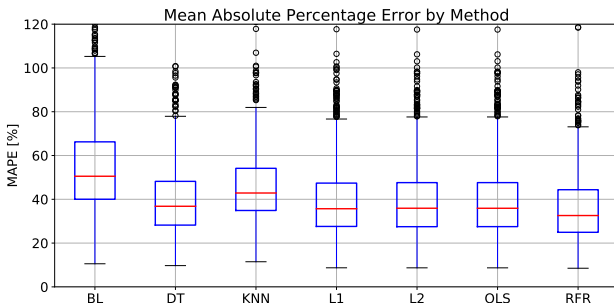


Figure: MAPEs by Prediction Method

- CAISO baseline performs worst

# Case Study on DR Program (cont'd)

## ITEs by Geographic Region

- Larger reductions in warmer regions

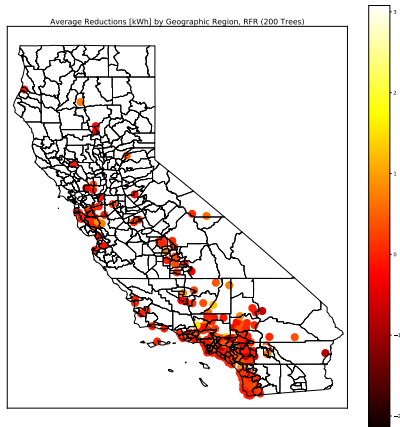


Figure: Geographic Distribution of ITEs

# Case Study on DR Program (cont'd)

## Average Treatment Effect Estimation

- Random Forest performs best
- Highest reductions in the evening
- Placebo events show  $\approx$  zero reduction

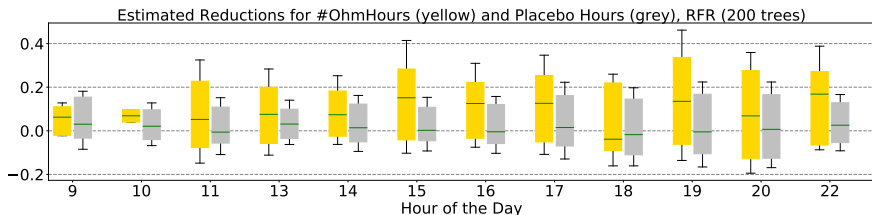


Figure: Estimated Reductions by Hour of the Day

# Case Study on DR Program (cont'd)

## Types of Load Shapes

- Morning + evening peak
- Daytime peak
- Night peak
- Evening peak

## Interesting Observation

- Users with higher entropy reduce more

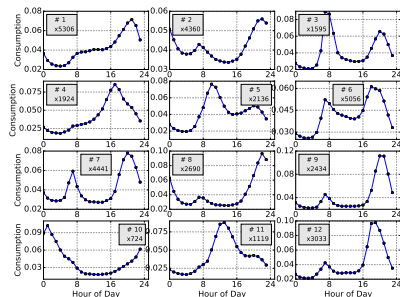


Figure: Characteristic Load Shapes

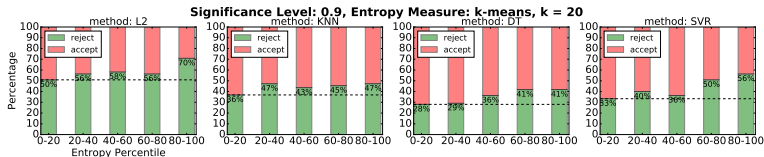


Figure: Percentage of Rejected Nulls vs. Forecasting Method

# Conclusion

- Description of Residential Demand Response using ordinary machine learning methods
- Estimation of counterfactual consumption during DR events
- Presented Black-box Machine Learning Methods
  - OLS, L1, L2, KNN, DT, RFR
  - Random Forest has lowest MAPE
- Identified “dictionary” of load shapes to compute variability of consumption
- Discovered a higher percentage of reduction among more variable users

# Further Work

## Completed/In Progress

- Improve estimation of counterfactual by using **latent variables**<sup>4</sup>
  - Hidden Markov Model
  - Mixture Models
- Nonparametric Estimators<sup>5</sup>
- Analysis of bias and variance in estimation process<sup>5</sup>
- Mechanism Design for DR elicitation

## Upcoming

- Time series modeling to estimate causal impact of DR interventions
- Run **Randomized Control Trial (RCT)** to
  - Validate non-experimental estimates of DR reduction
  - Target most susceptible users for DR incentives

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<sup>4</sup>D. Zhou, M. Balandat, C. Tomlin: A Bayesian Perspective on Residential Demand Response Using Smart Meter Data. 54th Annual Allerton Conference on Communication, Control, and Computing, September 2016

<sup>5</sup>M. Balandat: PhD Thesis. University of California, Berkeley, 2016

Thank You!  
Questions?